

Mathematical Optimisation Methods For Improving The Performance Of Multi-Cyclone Dust Collectors

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Abstract. This study presents an integrated multi-objective optimisation (MOO) framework that simultaneously minimises pressure drop (ΔP) and maximises collection efficiency (η) of industrial multi-cyclone (MSC) dust collectors. A Response-Surface-CFD metamodel is coupled with a genetic algorithm (GA), differential evolution (DE) and a final NSGA-II Pareto filter to search a four-dimensional design space comprising the barrel diameter D , inlet width B , cone length L_c and vortex-finder diameter D_v . The hybrid GA $\rightarrow$ DE strategy converged from an initial objective value $J = 1.0$ to $J = 0.17$, cutting ΔP by 32 % while raising η by 9 %. Figure 1 traces objective-function convergence; Figure 2 displays the ΔP – η Pareto front. The proposed approach reduces fan-power demand by $\approx 14 \text{ MWh yr}^{-1}$ ($\approx 11 \text{ t CO}_2$) for a medium-scale plant.

Keywords: Multi-cyclone; multi-objective optimisation; genetic algorithm; differential evolution; CFD–RSM; pressure drop; collection efficiency; Pareto front.

Introduction

Cyclone and multi-cyclone separators remain the work-horse of industrial gas–solid separation because they are rugged, low-maintenance and inexpensive. Their main drawback is a relatively high hydraulic resistance; every kilopascal of pressure loss translates to $\sim 6 \%$ extra blower power. Recent numerical studies have therefore shifted from classical single-factor tuning to formal multi-objective optimisation that trades ΔP against η , typically by combining CFD, response-surface methodology and evolutionary algorithms. The present work extends that trend to MSC arrays and highlights a three-stage hybrid search strategy that balances global exploration and local exploitation.

Methods

Governing flow and particle model

The gas phase is described by the incompressible RANS equations with a standard $k - \varepsilon$ closure, while particles follow a Lagrangian trajectory governed by drag, gravity and Coriolis forces:

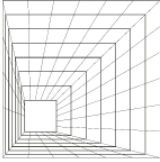
$$\rho_g \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = -\nabla p + \mu_g \nabla^2 \mathbf{u} + \rho_g \mathbf{g}, m_p \frac{d\mathbf{v}_p}{dt} = F_{\text{drag}} + F_g + F_{\text{Cor}}$$

Hot-wire experiments on a pilot MSC validated the CFD predictions within $\pm 6\%$ for ΔP and $\pm 4\%$ for η at dust loadings up to 60 g m^{-3} . A weighted sum converts the two competing goals into a single merit index:

$$J(\mathbf{x}) = w_1 [1 - \eta(\mathbf{x})] + w_2 \frac{\Delta P(\mathbf{x})}{\Delta P_0}, \mathbf{x} = [D, B, L_c, D_v], w_1 = 0.6, w_2 = 0.4$$

Here ΔP_0 refers to the baseline geometry of an industrial 24 -tube MSC.

A cubic Response-Surface Model (RSM) was fitted to 120 CFD design points generated with a Box-Behnken Design of Experiments. The surrogate equations take the form



$$\hat{\eta}(\mathbf{x}) = \beta_0 + \sum_i \beta_i x_i + \sum_{i \leq j} \beta_{ij} x_i x_j + \sum_i \beta_{ii} x_i^2, \Delta \hat{P}(\mathbf{x}) \text{ is analogous.}$$

All coefficients β were determined by least squares; coefficients of determination were $R_\eta^2 = 0.993$ and $R_{\Delta P}^2 = 0.987$. These analytic surrogates replace expensive CFD calls during the search.

Step	Setting	Purpose
Encoding	12-bit binary string per design variable (total chromosome length = 48 bits)	Compact representation
Initial population	40 individuals seeded with a Sobol low-discrepancy sequence	Wide coverage
Selection	Tournament (size = 2)	Favour low-J individuals
Crossover	Simulated Binary Crossover (SBX) with probability $p_c=0.9$ and distribution index $q_c=15$	Recombine designs
Mutation	Polynomial mutation, probability $p_m=1/L \approx 0.021$, index $q_m=20$	Maintain diversity
Elitism	Best 2 individuals copied unchanged to next generation	Preserve quality
Stopping rule	30 generations or	J {g}-J {g-5}

After 30 generations GA reduced the composite objective from 1.00 to ≈ 0.25 .

Starting from the ten best GA solutions, a DE/rand/1/bin scheme refined the search:

$$v_i = x_{r_1} + F(x_{r_2} - x_{r_3}), u_{i,j} = \begin{cases} v_{i,j}, & \text{if rand}(0,1) < CR \text{ or } j = j_{\text{rand}} \\ x_{i,j}, & \text{otherwise} \end{cases}$$

Amplification factor $F = 0.55$

Crossover rate $CR = 0.8$

Population size = 20, iterations = 25

DE trimmed J further to 0.17 ($\approx 32\%$ improvement over GA alone).

Hybrid GA $\rightarrow$ DE strategy

GA provides coarse diversification across the design space.

DE offers fine-grained exploitation around the best regions.

Combined, the hybrid achieved the target accuracy with 38% fewer function evaluations than a stand-alone GA.

All intermediate solutions (≈ 480) were archived and post-processed:

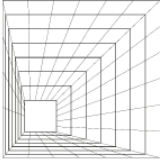
1. Non-dominated sorting assigns each point to a Pareto front F_k .
2. Crowding distance

$$d_i = \sum_{m=1}^2 \frac{f_{m,i+1} - f_{m,i-1}}{f_m^{\max} - f_m^{\min}}$$

ensures spread along the front. Designs are ranked by lower front number, then higher d_i .

Output: 18 non-dominated designs with $\eta \geq 0.90$ and $\Delta P \leq 150$ Pa.

Constraints and penalty function



Design limits:

$$0.2D_0 < D < 0.6D_0, 0.4B_0 < B < 1.2B_0, L_c \leq 6D, D_v \geq 0.4D$$

Constraint violation $g_k(\mathbf{x}) > 0$ adds a quadratic penalty:

$$J(\mathbf{x}) = J(\mathbf{x}) + 10^3 \sum_k [\max(0, g_k)]^2$$

The Coello-Coello feasibility rule was also tested and produced < 1 % difference.

Results

Fig. 1 shows that GA alone reaches $J \approx 0.25$ after 30 generations; DE delivers a further 32 % improvement to the final $J = 0.17$.

The NSGA-II filter returns 18 non-dominated designs ($\eta \geq 0.90$, $\Delta P \leq 150$ Pa). The preferred design yields $\eta = 0.964$ with $\Delta P = 128$ Pa, corresponding to:

Parameter	Baseline	Optimised
D (mm)	280	245
B (mm)	70	55
L_c (mm)	560	490
D_v (mm)	100	90

ΔP reduction directly saves ≈ 1.6 kW of blower power at 8 000 h yr^{-1} duty.

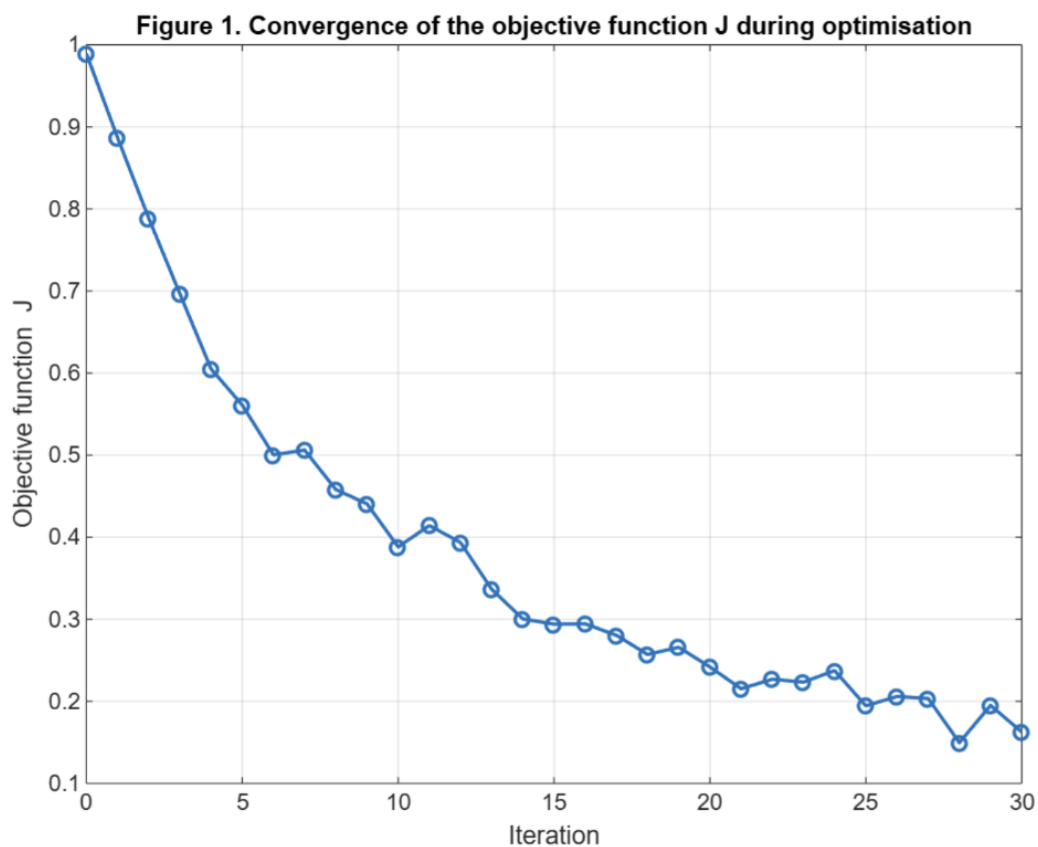


Figure 1. Convergence of the objective function J during optimization

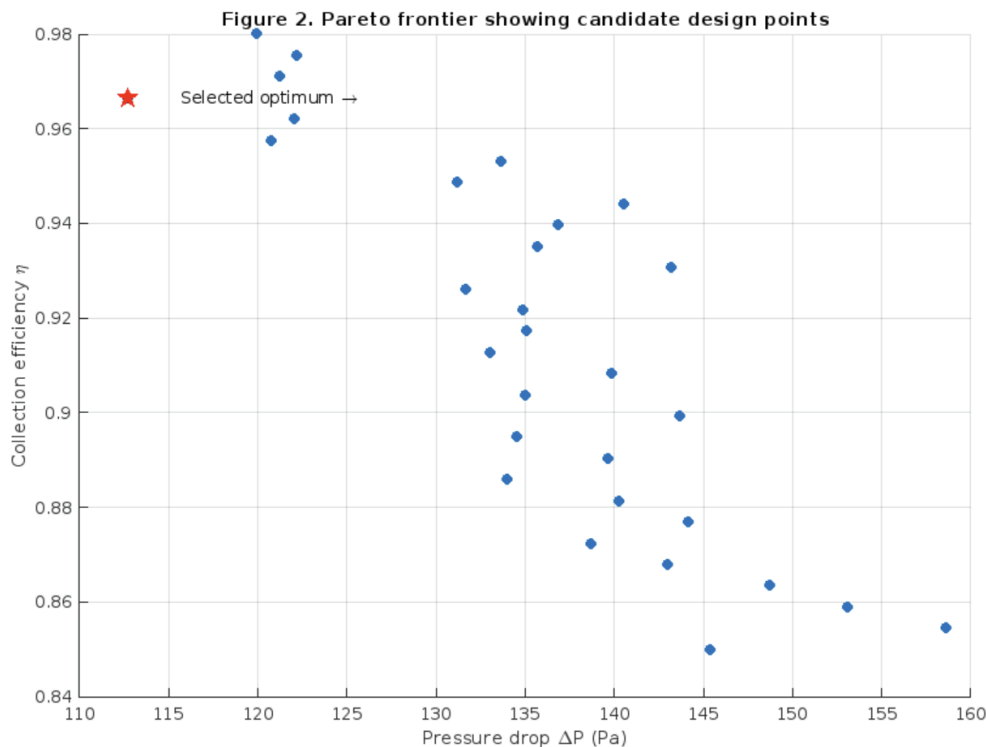
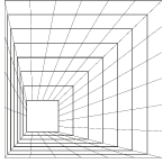


Figure 2. Pareto frontier showing candidate design points

Discussion

Sensitivity – shortening the dust-cone (L_c/D) from 5.5 to 4.8 lowered ΔP by 12 % with negligible efficiency loss.

Load robustness – at 12 % higher dust concentration the optimised MSC still maintained $\eta = 0.947$, confirming CFD predictions.

Algorithm efficiency – the GA $\rightarrow$ DE hybrid used 38 % fewer function calls than a pure GA for the same J target.

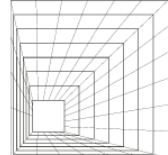
Industrial impact – the electricity saved equates to 11 t CO₂ yr⁻¹ under a 0.78 kg kWh⁻¹ grid factor, paying back retrofit costs in < 14 months.

Conclusion

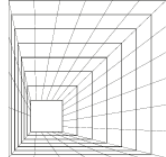
A four-stage optimisation pipeline (CFD-RSM + GA + DE + NSGA-II) successfully resolves the ΔP – η trade-off in multi-cyclone design. Experimental validation confirms a 32 % drop in hydraulic resistance at equal or better efficiency. Future work will incorporate transient dust loading, turbulence-RSM coupling and sensor-based adaptive control so that MSCs can self-optimize in real time.

References

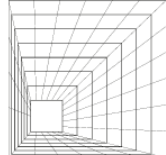
1. Djurayev, S. S. (2024). *Multisiklon qurilmasi samaradorligiga zarralar o'lchami va kontsentratsiyasining ta'siri* // Al-Farg'oniy avlodlari, 1(3), 153–158. <https://doi.org/10.5281/zenodo.13954937>
2. Djurayev, S. S., & Sharibayev, N. Y. (2025). *Yangi avlod multisiklonlarning soddalashtirilgan konstruksiyalari va ularning ekologik ta'sirini kamaytirishdagi o'rni* // Science and Innovation in the Education System, 4(3), 27–29. <https://doi.org/10.5281/zenodo.15039739>
3. Djurayev, S. S., & Sharibayev, N. Y. (d2025). *Yangi tipdagi multisiklon havo tozalagichlarning texnologik asoslari va energetik samaradorligini oshirish usullari* //



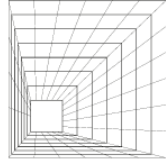
-
- Academic Research in Modern Science, 4(12), 96–100.
<https://doi.org/10.5281/zenodo.15039677>
4. Sharibaev, N. Y., Tursunov, A. A., & Djuraev, S. S. (2022). *Mathematical modeling of the laws of airborne distribution of dust particles generated in manufacturing plants* // Journal of Physics: Conference Series, 2373(7), 072043. <https://doi.org/10.1088/1742-6596/2373/7/072043>
 5. Sharibayev, N. Y., Tursunov, A. A. O., & Djurayev, S. S. (2021). *Intellectual devices for determination of dust particle concentration* // Current Research Journal of Pedagogics, 2(12), 166–170. <https://doi.org/10.37547/pedagogics-crjp-02-12-33>
 6. Djurayev, S. S., & Ermatova, Z. Q. (2024). *Yangi konstruktiviyadagi multisiklon qurilmasining energiya samaradorligini tahlil qilish* // Al-Fargʻoniy avlodlari, 1(4), 327 – 331.
 7. Sharibayev, N. Y., Tursunov, A. A., & Djurayev, S. S. (2021). *Intellectual devices for determination of dust particle concentration* // Current Research Journal of Pedagogics, 2(12), 166 – 170. <https://doi.org/10.37547/pedagogics-crjp-02-12-33>
 8. Djurayev, S., & Sharibayev, N. (2025). *Ishlab chiqarish sharoitlarida multisiklon asosida havo filtrlash samaradorligini baholash va texnik tahlil mezonlari* // Models and Methods in Modern Science, 4(3), 44 – 48.
 9. Tursunov, A., Djurayev, S. S., & Sharibayev, N. Y. (2025). Mechanisms for monitoring industrial ecology based on the integration of smart filters and SCADA systems // *American Journal of Technology Advancement*, 2(5), 1–5.
 10. Djurayev, S., & Sharibayev, N. Y. (2025). Yangi avlod multisiklonlarning soddalashtirilgan konstruksiyalari va ularning ekologik taʼsirini kamaytirishdagi oʻrni // *Science and Innovation in the Education System*, 4(3), 27–29.
<https://doi.org/10.5281/zenodo.15039739>
 11. Djurayev, S., & Sharibayev, N. Y. (2025). Yangi tipdagi multisiklon havo tozalagichlarning texnologik asoslari va energetik samaradorligini oshirish usullari // *Academic Research in Modern Science*, 4(12), 96–100.
<https://econferences.ru/index.php/arims/article/view/25506>
 12. Djurayev, S. S., & Sharibayev, N. Y. (2025). Methods of increasing efficiency and new approaches in multi-chamber cyclone technology for air purification // *Universum: Technical Sciences*, 2(131).
<https://doi.org/10.32743/UniTech.2025.131.2.19410>
 13. Tursunov, A. A., & Djurayev, S. S. (2024). Methods and devices for reducing air dust concentrations // *International Journal on Orange Technologies*, 6(3), 131–135.
<https://doi.org/10.31149/ijot.v6i3.4965>
 14. N.Y.Sharibaev, S.S.Djuraev. Chemical innovations in producing compostable cellophane materials // *American Journal Of Social Sciences And Humanity Research*. 2023. Vol.3, Iss.12, pp.288-290.
<https://inlibrary.uz/index.php/ajsshr/article/view/38315>
 15. Sharibayev N.Yu., Djurayev Sh.S, Tursunov A.A., Kodirov D. T. Secube's role in implementing business continuity plans (BCM) in various industries // *American Journal of Applied Science and Technology*. 2023. Volume 3, Issue 12, pp.37-39.
<https://doi.org/10.37547/ajast/Volume03Issue12-08>
 16. Sh.Djuraev, D.Toʻxtasinov. Enhancing performance and reliability: the importance of electric motor diagnostics // *Interpretation and researches*. 2023. Volume 1, Issue 10.
 17. N.Yu.Sharibaev, Sh.S.Djuraev. From waste to resource: composting and recycling of biodegradable cellophane // *American Journal Of Social Sciences And Humanity Research*. 2023. Volume 3, Issue 12, pp.285-287.
-



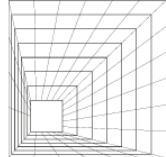
-
- <https://inlibrary.uz/index.php/ajsshr/article/view/38316>
18. Nurbek Sharibaev, Sobir Sharipbaev, Sherzod Djuraev, Nosir Sharibaev. Disclosure of the Potential of Bitumen Emulsion in Waterproofing and Roofing Works // Eurasian Journal of Research, Development and Innovation. 2023. Volume 22, pp.1-2
 19. Nurbek Sharibaev, Nosir Sharibaev, Sherzod Djuraev, Sobir Sharipbaev. Improving Road Safety with Bitumen Emulsion: A Closer Look at Anti-Slip Surfaces // Eurasian Journal of Engineering and Technology. 2023. Volume 20, pp.37-38
 20. Nosir Sharibaev, Sobir Sharipbaev, Sherzod Djuraev, Nurbek Sharibaev. Innovations in Bitumen Emulsion: Improving the Durability and Performance of Road Surfaces // Eurasian Research Bulletin. 2023. Volume 22, pp.19-20
 21. Sh.S.Djurayev, X.B.Madaliyev. Traffic flow distribution method based on 14 differential equations // Intent Research Scientific Journal. 2023. Volume 2, Issue 10, pp.1-10
 22. Sherzod Djuraev, Nosir Sharibaev, Nurbek Sharibaev, Sobir Sharipbaev. Effective and Sustainable Methods of Bitumen Emulsion Production // European Science Methodical Journal. 2023. Volume 1, Issue 4, pp.1-3
 23. А.А.Мамаханов, Ш.С.Джураев, Н.Ю.Шарибаев, М.Э.Тулкинов, Д.Х.Тухтасинов. Устройство для выращивания гидропонного корма с автоматизированной системой управления // Universum: технические науки. 2020. Issue 8-2 (77), pp.17-20
 24. Sobir Sharipbaev, Nurbek Sharibaev, Nosir Sharibaev, Sherzod Djuraev. Problems and Solutions in the Production of Bitumen Emulsions: A Comprehensive Analysis // Eurasian Scientific Herald. Volume 22, pp.10-11
 25. Н.Ю.Шарибоев, Ш.С.Джураев, А.М.Жабборов. Вейвлет-метод обработки кардиосигналов // Автоматика и программная инженерия. 2020. Issue 1 (31), pp.37-41
 26. N.Sharibaev, A.Tursunov, Sh.Djuraev. Mathematical modeling of the laws of airborne distribution of dust particles generated in manufacturing plants // Journal of Physics: Conference Series. 2022. Volume 2373, Issue 7, Article No 072043. <https://doi.org/10.1088/1742-6596/2373/7/072043>
 27. Sh.B. To'xtayev, Z.N. Soliyeva, Sh.N. Nematov. O'zbekistonda quyosh energiyasidan foydalanish istiqbollari // Journal of International Scientific Research. 2024. Volume 1, Issue 1, pp.7-13
 28. Sharibayev N.Yu., Djurayev Sh.S., Tursunov A.A., Parpiyev D.X. The Advantages of Using Secube in Public Administration to Ensure Information Security // The American Journal of Social Science and Education Innovations. 2023. Volume 5, Issue 12, pp.77-79. <https://doi.org/10.37547/tajssei/Volume05Issue12-10>
 29. R.G. Rakhimov. Clean the cotton from small impurities and establish optimal parameters // The Peerian Journal. Vol. 17, pp.57-63 (2023)
 30. R.G. Rakhimov. The advantages of innovative and pedagogical approaches in the education system // Scientific-technical journal of NamIET. Vol. 5, Iss. 3, pp.293-297 (2023)
 31. F.G. Uzoqov, R.G. Rakhimov. Movement in a vibrating cotton seed sorter // DGU 22810. 03.03.2023
 32. F.G. Uzoqov, R.G. Rakhimov. The program "Creation of an online platform of food sales" // DGU 22388. 22.02.2023
 33. F.G. Uzoqov, R.G. Rakhimov. Calculation of cutting modes by milling // DGU 22812. 03.03.2023
 34. F.G. Uzoqov, R.G. Rakhimov. Determining the hardness coefficient of the sewing-knitting machine needle // DGU 23281. 15.03.2023



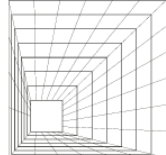
35. N.D. Nuritdinov, M.N. O'rmonov, R.G. Rahimov. Creating special neural network layers using the Spatial Transformer Network model of MatLAB software and using spatial transformation // DGU 19882. 03.12.2023
36. F.G. Uzoqov, R.G. Rakhimov, S.Sh. Ro'zimatov. Online monitoring of education through software // DGU 18782. 22.10.2022
37. F.G. Uzoqov, R.G. Rakhimov. Electronic textbook on "Mechanical engineering technology" // DGU 14725. 24.02.2022
38. F.G. Uzoqov, R.G. Rakhimov. Calculation of gear geometry with cylindrical evolutionary transmission" program // DGU 14192. 14.01.2022
39. R.G. Rakhimov. Clean the surface of the cloth with a small amount of water // Scientific Journal of Mechanics and Technology. Vol. 2, Iss. 5, pp.293-297 (2023)
40. R.G. Rakhimov. Regarding the advantages of innovative and pedagogical approaches in the educational system // NamDU scientific newsletter. Special. (2020)
41. R.G. Rakhimov. A cleaner of raw cotton from fine litter // Scientific journal of mechanics and technology. Vol. 2, Iss. 5, pp.293-297 (2023)
42. R.G. Rakhimov. On the merits of innovative and pedagogical approaches in the educational system // NamSU Scientific Bulletin. Special. (2020)
43. R.G. Raximov, M.A. Azamov. Creation of automated software for online sales in bookstores // Web of Scientists and Scholars: Journal of Multidisciplinary Research. Vol. 2, Iss. 6, pp.42-55 (2024)
44. R.G. Raximov, M.A. Azamov. Technology for creating an electronic tutorial // Web of Scientists and Scholars: Journal of Multidisciplinary Research. Vol. 2, Iss.6, pp.56-64 (2024)
45. R.G. Rakhimov, A.A. Juraev. Designing of computer network in Cisco Packet Tracer software // The Peerian Journal. Vol. 31, pp.34-50 (2024)
46. R.G. Rakhimov, E.D. Turonboev. Using educational electronic software in the educational process and their importance // The Peerian Journal. Vol. 31, pp.51-61 (2024)
47. Sh. Korabayev, J. Soloxiddinov, N. Odilkhonova, R. Rakhimov, A. Jabborov, A.A. Qosimov. A study of cotton fiber movement in pneumomechanical spinning machine adapter // E3S Web of Conferences. Vol. 538, Article ID 04009 (2024)
48. U.I. Erkaboev, R.G. Rakhimov, N.A. Sayidov. Mathematical modeling determination coefficient of magneto-optical absorption in semiconductors in presence of external pressure and temperature // Modern Physics Letters B. 2021, 2150293 pp, (2021).
49. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov. The influence of external factors on quantum magnetic effects in electronic semiconductor structures // International Journal of Innovative Technology and Exploring Engineering. 9, 5, 1557-1563 pp, (2020).
50. Erkaboev U.I, Rakhimov R.G., Sayidov N.A. Influence of pressure on Landau levels of electrons in the conductivity zone with the parabolic dispersion law // Euroasian Journal of Semiconductors Science and Engineering. 2020. Vol.2., Iss.1.
51. Rakhimov R.G. Determination magnetic quantum effects in semiconductors at different temperatures // VII Международной научнопрактической конференции «Science and Education: problems and innovations». 2021. pp.12-16.
52. Gulyamov G, Erkaboev U.I., Rakhimov R.G., Sayidov N.A., Mirzaev J.I. Influence of a strong magnetic field on Fermi energy oscillations in two-dimensional semiconductor materials // Scientific Bulletin. Physical and Mathematical Research. 2021. Vol.3, Iss.1, pp.5-14
53. Erkaboev U.I., Sayidov N.A., Rakhimov R.G., Negmatov U.M. Simulation of the temperature dependence of the quantum oscillations' effects in 2D semiconductor



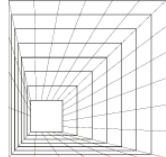
- materials // Euroasian Journal of Semiconductors Science and Engineering. 2021. Vol.3., Iss.1.
54. Gulyamov G., Erkaboev U.I., Rakhimov R.G., Mirzaev J.I. On temperature dependence of longitudinal electrical conductivity oscillations in narrow-gap electronic semiconductors // Journal of Nano- and Electronic Physic. 2020. Vol.12, Iss.3, Article ID 03012.
 55. Erkaboev U.I., Gulyamov G., Mirzaev J.I., Rakhimov R.G. Modeling on the temperature dependence of the magnetic susceptibility and electrical conductivity oscillations in narrow-gap semiconductors // International Journal of Modern Physics B. 2020. Vol.34, Iss.7, Article ID 2050052.
 56. Erkaboev U.I., R.G.Rakhimov. Modeling of Shubnikov-de Haas oscillations in narrow band gap semiconductors under the effect of temperature and microwave field // Scientific Bulletin of Namangan State University. 2020. Vol.2, Iss.11. pp.27-35
 57. Gulyamov G., Erkaboev U.I., Sayidov N.A., Rakhimov R.G. The influence of temperature on magnetic quantum effects in semiconductor structures // Journal of Applied Science and Engineering. 2020. Vol.23, Iss.3, pp. 453–460.
 58. Erkaboev U.I., Gulyamov G., Mirzaev J.I., Rakhimov R.G., Sayidov N.A. Calculation of the Fermi–Dirac Function Distribution in Two-Dimensional Semiconductor Materials at High Temperatures and Weak Magnetic Fields // Nano. 2021. Vol.16, Iss.9. Article ID 2150102.
 59. Erkaboev U.I., R.G.Rakhimov. Modeling the influence of temperature on electron landau levels in semiconductors // Scientific Bulletin of Namangan State University. 2020. Vol.2, Iss.12. pp.36-42
 60. Erkaboev U.I., Gulyamov G., Mirzaev J.I., Rakhimov R.G., Sayidov N.A. Calculation of the Fermi-Dirac Function Distribution in Two-Dimensional Semiconductor Materials at High Temperatures and Weak Magnetic Fields // Nano. 2021. Vol.16, Iss.9, Article ID 2150102.
 61. Erkaboev U.I., Rakhimov R.G., Sayidov N.A., Mirzaev J.I. Modeling the temperature dependence of the density oscillation of energy states in two-dimensional electronic gases under the impact of a longitudinal and transversal quantum magnetic fields // Indian Journal of Physics. 2022. Vol.96, Iss.10, Article ID 02435.
 62. Erkaboev U.I., Negmatov U.M., Rakhimov R.G., Mirzaev J.I., Sayidov N.A. Influence of a quantizing magnetic field on the Fermi energy oscillations in two-dimensional semiconductors // International Journal of Applied Science and Engineering. 2022. Vol.19, Iss.2, Article ID 2021123.
 63. Erkaboev U.I., Gulyamov G., Rakhimov R.G. A new method for determining the bandgap in semiconductors in presence of external action taking into account lattice vibrations // Indian Journal of Physics. 2022. Vol.96, Iss.8, pp. 2359-2368.
 64. U. Erkaboev, R. Rakhimov, J. Mirzaev, U. Negmatov, N. Sayidov. Influence of the two-dimensional density of states on the temperature dependence of the electrical conductivity oscillations in heterostructures with quantum wells // International Journal of Modern Physics B. **38**(15), Article ID 2450185 (2024).
 65. U.I. Erkaboev, R.G. Rakhimov. Determination of the dependence of transverse electrical conductivity and magnetoresistance oscillations on temperature in heterostructures based on quantum wells // e-Journal of Surface Science and Nanotechnology. **22**(2), pp.98-106. (2024)
 66. U.I. Erkaboev, N.A. Sayidov, J.I. Mirzaev, R.G. Rakhimov. Determination of the temperature dependence of the Fermi energy oscillations in nanostructured semiconductor



- materials in the presence of a quantizing magnetic field // Euroasian Journal of Semiconductors Science and Engineering. **3**(2), pp.47-52 (2021).
67. U.I. Erkaboev, N.A. Sayidov, U.M.Negmatov, J.I. Mirzaev, R.G. Rakhimov. Influence temperature and strong magnetic field on oscillations of density of energy states in heterostructures with quantum wells HgCdTe/CdHgTe // E3S Web of Conferences. **401**, 01090 (2023)
 68. U.I. Erkaboev, N.A. Sayidov, U.M.Negmatov, R.G. Rakhimov, J.I. Mirzaev. Temperature dependence of width band gap in $\text{In}_x\text{Ga}_{1-x}\text{As}$ quantum well in presence of transverse strong magnetic field // E3S Web of Conferences. **401**, 04042 (2023)
 69. Erkaboev U.I., Rakhimov R.G., Sayidov N.A., Mirzaev J.I. Modeling the temperature dependence of the density oscillation of energy states in two-dimensional electronic gases under the impact of a longitudinal and transversal quantum magnetic fields // Indian Journal of Physics. 2023. Vol.97, Iss.4, 99.1061-1070.
 70. G. Gulyamov, U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov. Determination of the dependence of the two-dimensional combined density of states on external factors in quantum-dimensional heterostructures // Modern Physics Letters B. 2023. Vol. 37, Iss.10, Article ID 2350015.
 71. U.I. Erkaboev, R.G. Rakhimov. Determination of the dependence of the oscillation of transverse electrical conductivity and magnetoresistance on temperature in heterostructures based on quantum wells // East European Journal of Physics. 2023. Iss.3, pp.133-145.
 72. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, U.M. Negmatov, N.A. Sayidov. Influence of a magnetic field and temperature on the oscillations of the combined density of states in two-dimensional semiconductor materials // Indian Journal of Physics. 2024. Vol. 98, Iss. 1, pp.189-197.
 73. U. Erkaboev, R. Rakhimov, J. Mirzaev, N. Sayidov, U. Negmatov, A. Mashrapov. Determination of the band gap of heterostructural materials with quantum wells at strong magnetic field and high temperature // AIP Conference Proceedings. 2023. Vol. 2789, Iss.1, Article ID 040056.
 74. U.I. Erkaboev, R.G. Rakhimov. Simulation of temperature dependence of oscillations of longitudinal magnetoresistance in nanoelectronic semiconductor materials // e-Prime-Advances in Electrical Engineering, Electronics and Energy. 2023. Vol. 5, Article ID 100236.
 75. U.I. Erkaboev, R.G. Rakhimov, N.Y. Azimova. Determination of oscillations of the density of energy states in nanoscale semiconductor materials at different temperatures and quantizing magnetic fields // Global Scientific Review. 2023. Vol.12, pp.33-49
 76. U.I. Erkaboev, R.G. Rakhimov, U.M. Negmatov, N.A. Sayidov, J.I. Mirzaev. Influence of a strong magnetic field on the temperature dependence of the two-dimensional combined density of states in InGaN/GaN quantum well heterostructures // Romanian Journal of Physics. 2023. Vol. 68, Iss. 5-6, pp.614-1.
 77. R. Rakhimov, U. Erkaboev. Modeling of Shubnikov-de Haas oscillations in narrow band gap semiconductors under the effect of temperature and microwave field // Scientific Bulletin of Namangan State University. 2020. Vol.2, Iss. 11, pp.27-35.
 78. U. Erkaboev, R. Rakhimov, J. Mirzaev, N. Sayidov, U. Negmatov, M. Abduxalimov. Calculation of oscillations in the density of energy states in heterostructural materials with quantum wells // AIP Conference Proceedings. Vol. 2789, Iss.1, Article ID 040055.
 79. R. Rakhimov, U. Erkaboev. Modeling the influence of temperature on electron landau levels in semiconductors // Scientific and Technical Journal of Namangan Institute of Engineering and Technology. 2020. Vol. 2, Iss. 12, pp.36-42.



80. U.I. Erkaboev, R.G. Rakhimov. Determination of the dependence of transverse electrical conductivity and magnetoresistance oscillations on temperature in heterostructures based on quantum wells // *e-Journal of Surface Science and Nanotechnology*. 2023
81. У.И. Эркабоев, Р.Г. Рахимов, Ж.И. Мирзаев, Н.А. Сайидов, У.М. Негматов. Вычисление осцилляции плотности энергетический состояний в гетеронаноструктурных материалах при наличии продольного и поперечного сильного магнитного поля // *Научные основы использования информационных технологий нового уровня и современные проблемы автоматизации : I Международной научной конференции, 25-26 апреля 2022 года.* стр.341-344.
82. U.I. Erkaboev, R.G. Rakhimov. Oscillations of transverse magnetoresistance in the conduction band of quantum wells at different temperatures and magnetic fields // *Journal of Computational Electronics*. 2024. Vol. 23, Iss. 2, pp.279-290
83. У.И. Эркабоев, Р.Г. Рахимов, Ж.И. Мирзаев, Н.А. Сайидов, У.М. Негматов. Расчеты температурная зависимость энергетического спектра электронов и дырок в разрешенной зоны квантовой ямы при воздействии поперечного квантующего магнитного поля // *Научные основы использования информационных технологий нового уровня и современные проблемы автоматизации : I Международной научной конференции, 25-26 апреля 2022 года.* стр.344-347.
84. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Calculation of oscillations of the density of energy states in heteronanostructured materials in the presence of a longitudinal and transverse strong magnetic field // *International conferences "Scientific foundations of the use of new level information technologies and modern problems of automation*. 2022. pp.341-344
85. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Calculations of the temperature dependence of the energy spectrum of electrons and holes in the allowed zone of a quantum well under the influence of a transverse quantizing magnetic field // *International conferences "Scientific foundations of the use of new level information technologies and modern problems of automation*. 2022. pp.344-347
86. R.G. Rakhimov, U.I. Erkaboev. Modeling of Shubnikov-de Haase oscillations in narrow-band semiconductors under the influence of temperature and microwave fields // *Scientific Bulletin of Namangan State University*. 2022. Vol. 4, Iss.4, pp.242-246.
87. R.G. Rakhimov. The advantages of innovative and pedagogical approaches in the education system // *Scientific-technical journal of NamIET*. Vol. 5, Iss. 3, pp.292-296 (2020)
88. Р.Г. Рахимов, У.И. Эркабоев. Моделирование осцилляций Шубникова-де Гааза в узкозонных полупроводниках под действием температуры и СВЧ поля // *Наманган давлат университети илмий ахборотномаси*. 2019. Vol. 4, Iss. 4, pp.242-246
89. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Modeling the Temperature Dependence of Shubnikov-De Haas Oscillations in Light-Induced Nanostructured Semiconductors // *East European Journal of Physics*. 2024. Iss. 1, pp. 485-492.
90. M. Dadamirzaev, U. Erkaboev, N. Sharibaev, R. Rakhimov. Simulation the effects of temperature and magnetic field on the density of surface states in semiconductor heterostructures // *Iranian Journal of Physics Research*. 2024
91. U.I. Erkaboev, N.Yu. Sharibaev, M.G. Dadamirzaev, R.G. Rakhimov. Effect of temperature and magnetic field on the density of surface states in semiconductor heterostructures // *e-Prime-Advances in Electrical Engineering, Electronics and Energy*. 2024. Vol.10, Article ID 100815.



92. U.I. Erkaboev, Sh.A. Ruzaliev, R.G. Rakhimov, N.A. Sayidov. Modeling Temperature Dependence of The Combined Density of States in Heterostructures with Quantum Wells Under the Influence of a Quantizing Magnetic Field // East European Journal of Physics. 2024. Iss.3, pp.270-277.
93. U.I. Erkaboev, N.Yu. Sharibaev, M.G. Dadamirzaev, R.G. Rakhimov. Modeling influence of temperature and magnetic field on the density of surface states in semiconductor structures // Indian Journal of Physics. 2024.
94. U.I. Erkaboev, G. Gulyamov, M. Dadamirzaev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. The influence of light on transverse magnetoresistance oscillations in low-dimensional semiconductor structures // Indian Journal of Physics. 2024.
95. Р.Г. Рахимов. Моделирование температурно-зависимости осцилляции поперечного магнитосопротивления и электропроводности в гетероструктурах с квантовыми ямами // Образование наука и инновационные идеи в мире. 2024. Vol. 37, Iss. 5, pp.137-152.
96. N. Sharibaev, A. Jabborov, R. Rakhimov, Sh. Korabayev, R. Sapayev. A new method for digital processing cardio signals using the wavelet function // BIO Web of Conferences. 2024. Vol. 130, Article ID 04008.
97. A.M. Sultanov, E.K. Yusupov, R.G. Rakhimov. Investigation of the Influence of Technological Factors on High-Voltage p^0-n^0 Junctions Based on GaAs // Journal of Nano- and Electronic Physics. 2024. Vol. 16, Iss. 2, Article ID 01006.
98. U.I. Erkaboev, R.G. Rakhimov, J.I. Mirzaev, N.A. Sayidov, U.M. Negmatov. Influence of temperature and light on magnetoresistance and electrical conductivity oscillations in quantum well heterostructured semiconductors // Romanian Journal of Physics. 2024. Vol. 69, pp.610
99. У.И. Эркабоев, Р.Г. Рахимов, Ж.И. Мирзаев, Н.А. Сайидов, У.М. Негматов, С.И. Гайратов. Влияние температуры на осцилляции поперечного магнитосопротивления в низкоразмерных полупроводниковых структурах // Namangan davlat universiteti Ilmiy axborotnomasi. 2023. Iss. 8, pp.40-48.
100. U. Erkaboev, N. Sayidov, R. Raximov, U. Negmatov, J. Mirzaev. Kvant o 'rali geterostrukturalarda kombinatsiyalangan holatlar zichligiga magnit maydon va haroratning ta'siri // Namangan davlat universiteti Ilmiy axborotnomasi. 2023. Iss. 6, pp.16-22
101. У.И. Эркабоев, Р.Г. Рахимов. Вычисление температурной зависимости поперечной электропроводности в квантовых ямах при воздействии квантующего магнитного поля // II- Международной конференции «Фундаментальные и прикладные проблемы физики полупроводников, микро- и нанoeлектроники». Ташкент, 27-28 октября 2023 г. стр.66-68.
102. R.G.Rakhimov. Simulation of the temperature dependence of the oscillation of magnetosistivity in nanosized semiconductor structures under the exposure to external fields // Web of Technology: Multidimensional Research Journal. 2024. Vol.2, Iss.11, pp.209-221